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## Mulliken symbol .

$A, B, E, T, A_{g}, A_{1 g}, A_{2 g}, B_{g}, B_{1 g}, B_{2 g}, A_{u}, B_{u}, E, E_{g}, T_{1 g}, T_{2 g} T_{2 u}$

What are a meaning of Mulliken symbols ?


## Mulliken symbolism Rules for Irreducible representation .

* Consider character table for $\mathrm{C}_{3 \mathrm{v}}$ point group .

| $C_{3 V}$ | $E$ | $2 C_{2}$ | $3 \sigma_{v}$ |
| :---: | :---: | :---: | :---: |
| $A_{1}$ | 1 | 1 | 1 |
| $A_{2}$ | 1 | 1 | -1 |
| $E$ | 2 | -1 | 0 |

* $\mathrm{A}_{1}, \mathrm{~A}_{2}$, E be the Mulliken symbol which has certain meaning

See the character under E class and represent symbol A, B, E and T using following rule.

1. Dimensionality Rule :

All one dimensional representation s are designated by either A or B symbol Two dimensional IRs representation $n$ is designated by $E$
Three dimensional IRs representation n is designated by T
2. See the character under Principle axis for labeling one dimensional A \& B
if $\quad \chi\left(\mathrm{C}_{\mathrm{n}}\right)=+1 \quad---------$ symmetric representation --- label A
if $\chi\left(\mathrm{C}_{\mathrm{n}}\right)=-1$----------- asymmetric representation --- label B
3. Numerical Subscript rule : $1 \& 2$ numerical subscript are attached A , B, T representation for that see the character under secondary axis $\mathrm{C}_{2}$
if $\chi\left(\mathrm{C}_{2}\right)=+1 \quad$----------- symmetric representation --- label ' 1 '
if $\chi\left(\mathrm{C}_{2}\right)=-1 \quad----------$ asymmetric representation --- label '2'
if Secondary axis is absent then see the character under vertical plane if $\chi\left(\sigma_{v}\right)=+1$----------- symmetric representation --- label "1" if $\chi\left(\sigma_{v}\right)=-1 \quad----------$ asymmetric representation --- label " 2 '
4. Alphabetical subscript rule : g \&u subscript are attached to A , B, T representation for that see the character under center of inversion (i) class
if $\chi(\mathrm{i})=+1 \quad$----------- symmetric representation --- label ' g 'subscript
if $\chi$ (i) =-1 ----------- asymmetric representation --- label 'u' subscript

Question1 : Transform the $\Gamma_{1}, \Gamma_{2}, \Gamma_{3}, \Gamma_{4}$ into Mulliken symbols of the following character table

Ex: 1
Ex: 2

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $C_{2 h}$ | $E$ | $C_{2}$ | i | $\sigma_{h}$ |
| $\Gamma_{1}$ | 1 | 1 | 1 | 1 |
| $\Gamma_{2}$ | 1 | -1 | 1 | -1 |
| $\Gamma_{3}$ | 1 | 1 | -1 | -1 |
| $\Gamma_{4}$ | 1 | -1 | -1 | 1 |


| $\mathrm{C}_{3 \mathrm{~V}}$ | E | $2 \mathrm{C}_{3}$ | $3 \sigma_{v}$ |
| :---: | :---: | :---: | :---: |
| $\Gamma_{1}$ | 1 | 1 | 1 |
| $\Gamma_{2}$ | 1 | 1 | -1 |
| $\Gamma_{3}$ | 2 | -1 | 0 |

## Direct product of irreducible representation :

|  |  |  |  | Direct |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}_{2 \mathrm{~V}}$ | E | $\mathrm{C}_{2}$ | $\sigma_{\mathrm{xz}}$ | $\sigma_{\mathrm{yz}}$ | product | | $\mathrm{A}_{1}$ | 1 | 1 | 1 |
| :---: | :---: | :---: | :---: |
| $\mathrm{~A}_{2}$ | 1 | 1 | -1 |
| $\mathrm{~B}_{1}$ | 1 | -1 | -1 |
| $\mathrm{~B}_{2}$ | 1 | -1 | 1 |
| $\mathrm{~A}_{1} \times \mathrm{A}_{2}$ | 1 | 1 | -1 |
| $\mathrm{~A}_{2} \times \mathrm{A}_{2}$ | 1 | 1 | -1 |
| $\mathrm{~A}_{2} \times \mathrm{B}_{1}$ | 1 | -1 | 1 |
|  |  |  |  |
|  |  |  |  |
|  |  |  | $\mathrm{~A}_{2}$ |
|  |  |  |  |

$$
\begin{aligned}
& \text { Product of Dimension : A, B, E, T } \\
& A \times A=A, B \times B=A \\
& A \times B=B \times A=B \\
& A \times E=B \times E=E \\
& E \times E=A+T \text { or } B+T \text { depend on } P . G \\
& E x T=A+E+T \\
& T \times T=A+E+T+T
\end{aligned}
$$

Product of subscript : 1,2,g,u

$$
1 \times 1=1
$$

$$
1 \times 2=1
$$

$$
g \times g=g
$$

$$
\mathrm{gxu}=\mathrm{u}
$$

$$
2 \times 2=1
$$

$$
\mathrm{uxu}=\mathrm{g}
$$

[symmetric]x[symmetri] = symmetric
[symmetric]x[asymmetri] = asymmetric
[asymmetric]×[asymmetric] = symmetric

## Standard reduction formula :

$$
\mathrm{n}\left(\Gamma_{\mathrm{i}}\right)=\left[\mathrm{g}(\mathrm{R}) \cdot \chi_{\mathrm{RR}}(\mathrm{R}) \cdot \chi_{\mathrm{RR}}(\mathbf{R})\right] / \mathrm{h}
$$

Where
$g(R)$ - multiplying factor of respective class
$\chi_{\mathrm{IR}}(\mathrm{R})$. - character if IRs representation under respective class
$\chi_{R R}(\mathrm{R}$ - character if RRs representation under respective class
h - order of group
Q1. Find out number of time $A_{1}, A_{2}, B_{1}$, and $B_{2}$ will appear in the following table order of group

| $\mathrm{C}_{2 \mathrm{~V}}$ | E | $\mathrm{C}_{2}$ | $\sigma_{\mathrm{xz}}$ | $\sigma_{\mathrm{yz}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{A}_{1}$ | 1 | 1 | 1 | 1 |
| $\mathrm{~A}_{2}$ | 1 | 1 | -1 | -1 |
| $\mathrm{~B}_{1}$ | 1 | -1 | 1 | -1 |
| $\mathrm{~B}_{2}$ | 1 | -1 | -1 | -1 |
| $\chi_{R R}(\mathrm{R})$ | 15 | -1 | 3 | 3 |

Q1. Find out number of time $\mathrm{A}_{1}, \mathrm{~A}_{2}, \mathrm{E}$ will appear in the following table order of group

| $\mathrm{C}_{3 \mathrm{~V}}$ | E | $2 \mathrm{C}_{3}$ | $3 \sigma_{\mathrm{v}}$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{A}^{2}$ | 1 | 1 | 1 |
|  |  |  |  |
| $\mathrm{~A}^{2}$ | 1 | 1 | -1 |
| E | 2 | -1 | 0 |
| $\chi_{\mathrm{RR}}(\mathrm{R})$ | 21 | 0 | 3 |

## THE END

