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Existence and Stability of Nonlocal Initial Value Problems Involving Generalized Katugampola Derivative

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Abstract:

In this paper, the existence results for the solutions to nonlocal initial value problems involving generalized Katugampola derivative are established. Some fixed point theorem techniques are used to derive the existence results. In the sequel, we investigate the generalized Ulam-Hyers-Rassias stability corresponding to our problem. Some examples are given to illustrate our main results.

Keywords:

Generalized Katugampola derivative, nonlocal initial value problem, Existence, Ulam-Hyers-Rassias stability.

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